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## KNOWLEDGE BASE APPLICATIONS TO ADAPTIVE SPACE-TIME PROCESSING, VOLUME IV: KNOWLEDGE-BASED TRACKING

**ITT Systems** 

**Technology Service Corporation** 

Charles Morgan and Lee Moyer

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testing of several knowledge-based rules.

Three types of tracking filters are described:

- 1. An uncoupled two-state alpha-beta filter with position and velocity component states,
- 2. An uncoupled three-state Kalman filter with position, velocity, and acceleration component states, and
- 3. An extended four-state Kalman filter with both x and y position and velocity component states.

The first two filters use a one-dimensional measurement vector containing the report position component. The extended Kalman filters uses a three-dimensional measurement vector containing x and y report position and "pseudo" Doppler, the latter defined as range times range rate.

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### 1.0 Introduction and Overview

The purpose of this effort has been to provide ITT Systems & Sciences with a knowledge based tracking capability that will support a space time adaptive processing (STAP) environment. This has included the development of a basic multiple target tracker and the design and testing of several knowledge based rules. A rule book containing 25 potential knowledge based rules was developed and is presented in Volume V.

For the purpose of ITT's application, the main elements of the tracker software can be imbedded in a larger STAP simulation by removing the GUI. The key tracking modules are setup\_Tracker\_6 and Run\_Tracker\_8.

The Run\_Tracker\_module allows the use of three types of tracking filters. These include:

- 1. an uncoupled two state alpha beta filter with position and velocity component states,
- 2. an uncoupled three state Kalman filter with position, velocity, and acceleration component states, and
- 3. an extended four Kalman filter with both x and y position and velocity component states.

The first two filters use a one dimensional measurement vector containing the report position component. The extended Kalman filter uses a three dimensional measurement vector containing x and y report position and "pseudo" Doppler, the latter defined as range times range rate.

The tracking software as delivered has been imbedded in a GUI structure that makes it easy to exercise the tracker under a variety of conditions. Using the GUI, the user can interactively select existing or new target scenarios and tracking options prior to tracker execution. Figure 1-1 shows the list of available options.

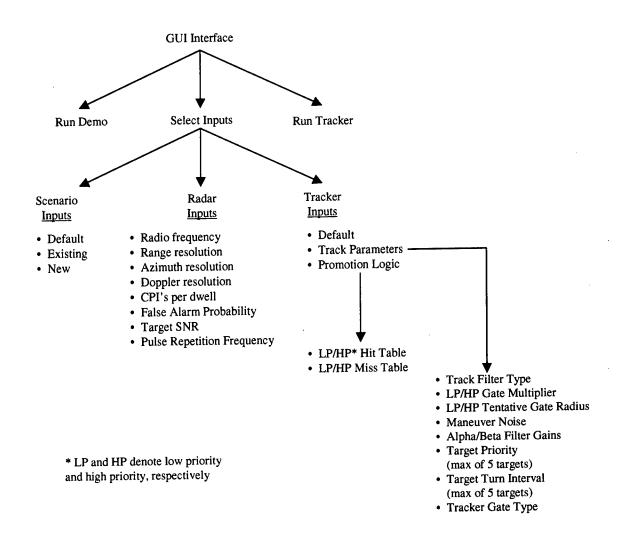


Figure 1-1: Tracker GUI Options

### 2.0 Tracker Description

The first part of this section contains a narrative description of the basic multiple target tracker. Detailed documentation has been provided in Section 3. This is followed by a discussion of three knowledge based tracking rules that can be used to support the STAP processor. Simple tracking simulations have been provided to illustrate the use of these rules.

#### 2.1 Basic Tracker

A high level description of the multiple target tracker function is shown below in Figure 2-1. The tracker processes reports on a per scan basis and makes use of a track table that contains several track attributes as well as kinematic information. The key attributes include the tracks identification number, its state value, which is a measure of track quality, and its status. Track status can be *dropped*, *tentative*, or *firm*. In the current software, a dropped status is assigned to a track whose state has been demoted to zero, a tentative status is assigned to a new

track formed by an unused report with a state value initialized to one, and a firm status is given to any track with a state value greater than one. The tracker's function consists of a correlation section together with association and track maintenance sections.

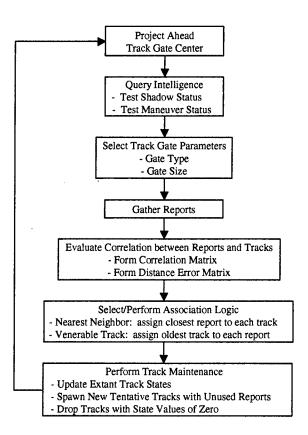


Figure 2-1: High Level Tracker Flow

The correlation section is performed by testing for inclusion each current report against each extrapolated track gate and forming a binary correlation matrix with ones in the capture positions. Tentative track gates formed from unassociated reports are extrapolated by centering a circle of kinematically-determined maximum radium about the report, whereas firm track gates are extrapolated by using the track filter prediction equations. Track gate sizes are typically a function of both the measurement and prediction uncertainties, as well as the track's maneuver status. A distance matrix of the same size as the correlation matrix is also formed containing the report-to-gate center distances.

The association and maintenance section uses the above correlation and distance error arrays to assign reports and tracks in a unique manner. In the even that multiple reports are common to a given track gate, or multiple tracks capture a common report, the association logic will resolve the conflict. Furthermore, any reports that are not assigned to an existing track will be used to spawn a new track designated to have a tentative status. Two simple association logics are currently available. There is a "nearest neighbor" logic that assigns the closest captured report to a given track and there is a "venerable track" logic that associates the oldest common track to a given report.

After all tracks and reports have been associated, the track state promotion logic is applied. Track states are updated using either a "hit" or a "miss" table, depending on whether they correlate with a report. These state tables are usually designed to require specified numbers of successive hits and misses before a track is declared as firm or dropped. Two examples are given below. In Case 1, tables Hit1 and Miss1 allow a tentative track to build up to firm status at state level 4 after three successive this, and to demote with each miss until it reaches state 0 where it is dropped. In Case 2, tables Hit2 and Miss2 show a more complex strategy. A tentative track promotes up to a firm status of 3 after two hits. However, there are hold states 4,5 and 6 which allow the track to recover its firm status more quickly after a single miss.

		Case 1		
State	1	2	3	4
Hit1	2	3	4	4
Miss1	0	1	2	3

			Case 2			
State	1	2	3	4	5	6
Hit2	2	3	3	5	3	3
Miss2	4	6	5	0	4	0

Once track state logic has been applied, the track table is updated. All tracks with state values of 0 are removed from the table. Furthermore, all reports that were not associated with extant tracks are used to spawn new tentative tracks that are added to the table.

### 2.2 Knowledge Based Rules

Knowledge based rules make use of extended map and intelligence information, and are used to improve the tracker's ability to support STAP processing requirements. Key issues include the tracking of targets in regions adjacent to large discretes, and in shadow zones that are blocked from the radar-s line of sight. Using map information the tracker should also be able to anticipate a target maneuver that will be required to avoid obstacles. Queued with this information, the tracker will apply appropriately shaped track gates that enhance its capability of capturing reports while maintaining reasonable gate sizes. Four rules are discussed below, along with simple tracking simulations.

In the following examples single target tracks are displayed graphically with the following conventions:

#### 2.2.1 Tracking Legend:

- + Predicted gate center position
- Measured report position
- o Coasted track position
- Extrapolated position of a missed detection
- d Dropped tentative track
- D# Dropped firm track
- # Corresponds to age (scans) of dropped track

In addition, all the results were obtained using an uncoupled Kalman tracking filter and all simulations assumed a ten second scan period.

#### 2.2.2 Maneuver/Obstacle Rules:

Both alpha beta and Kalman tracking filters do a good job with targets that move along a constant heading with a fixed speed. Deviations from a straight path cause prediction errors to occur and can ultimately result in a dropped track. Therefore it is important, whenever possible, to anticipate target maneuvers by several scans. This allows time to make such adjustments as increasing the gate size and track gain, or using a shaped gate to allow for across track deviations caused by target turning.

If a track approaches an obstacle whose across track extent is H, a maneuver can be anticipated to occur within a time extent no longer than  $T_{max}$ . For this discussion, assuming a constant target speed v and a maximum possible acceleration  $A_{max}$ , this extent is given by:

$$T_{\text{max}} = \frac{\rho}{v} \cos^{-1} (1 - H / \rho)$$

where

$$\rho = v^2 / A_{\text{max}}$$

denotes the radius of curvature of the target turn required to clear the obstacle. Somewhere within this time period the tracker should apply its maneuver logic.

Figures 2-2 to 2-4 use the same section of track to illustrate the effect of different gating strategies on the tracker's ability to handle a maneuvering target. Performance is computed for a constant speed (250 meters/sec), high SNR (20 dB at mid range) Swerling 1 target, as it approaches an obstacle (shaded rectangular region) from below and begins to turn after the twenty third scan.

Figure 2-2 shows the response of an uncompensated tracking filter using a standard track gate centered on the predicted gate center, and oriented along and across range with a size dependent on both the measurement and prediction errors. No target acceleration has been

assumed and no maneuver noise has been added. While the straight line section is handled adequately, the initial track begins to lose the target after the turn begins, whereupon it is demoted to a dropped status on the next four scans. The three kilometer circular gates indicate newly spawned tentative tracks that were subsequently updated to firm status.

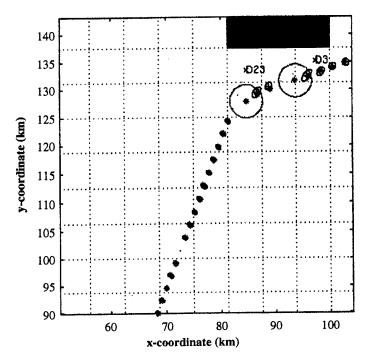


Figure 2-2: Uncompensated Tracker Response for Maneuvering Target

The first maneuvering target rule specifies the use of shaped elliptical gates. Figure 2-3 shows the same target as tracked using a combination of two gates, both centered on the predicted gate center. One gate is oriented along and across range, with a size determined by range and angle measurement uncertainties. The second gate is oriented along and across the targets instantaneous track and its size is a function of the maximum turning acceleration of the target, assumed here to be 0.5g units. Reports capture occurs if the measurement falls within either gate. Except for a missed report early in the linear part of the trajectory, causing the gate to swell initially and then settle down, the track is maintained throughout the maneuver. Each lower case d symbol indicates a dropped tentative track. This occurs when such a track fails to capture a report on the following scan. The large three kilometer circles denote tentative tracks that were successfully promoted to firm status. Finally, the dots occurring in both Figures 2-2 and 2-3, shown extrapolated from the straight line section of the approaching track, represent missed detections. While actual gates existed for these cases, they have been drawn here only or situations in which reports were captured.

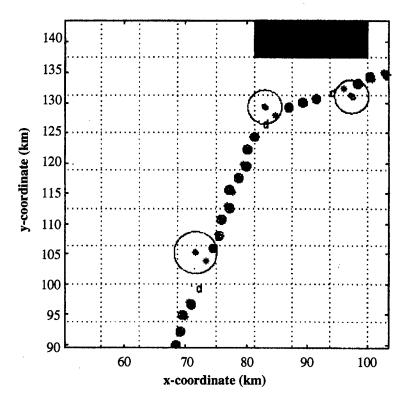


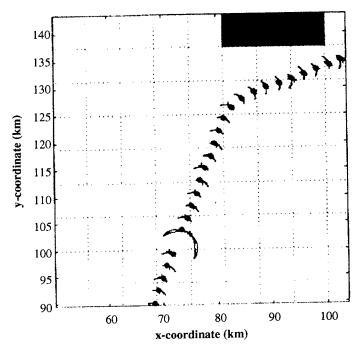
Figure 2-3: Compensated Tracker Response for Maneuvering Target.

Track Oriented Elliptical Gates used with 0.5g Across-Track Acceleration Allowance

The second maneuvering target rule specifies the use of a gate whose shape is determined solely by centripetal turning mechanics. Figure 2-4 shows the target being tracked using a "smile shaped" gate whose shape is determined by the kinematic constraints imposed on a constant speed target undergoing a centripetal maneuver. Let t range over the time interval from the last track update till the next predicted report acquisition, T<sub>scan</sub> seconds later. The maneuver envelope is given by the xy locus of points, oriented along and across the track, and generated by the equations:

$$x = vt + \rho \sin \theta$$
$$y = \rho (1 - \cos \theta)$$
$$\theta = v(T_{scan} - t)/\rho$$

where the radius of curvature  $\rho$  is defined as above. For this gate, a track capture occurs if the measurement ellipse, centered on the measured report and oriented along and across range, intersects the smile locus. As in the previous example, this gate is able to maintain the track throughout the target maneuver. One advantage of this gate is that is has a relatively small area as compared with other maneuver gates and this makes it less likely to capture any false alarms.

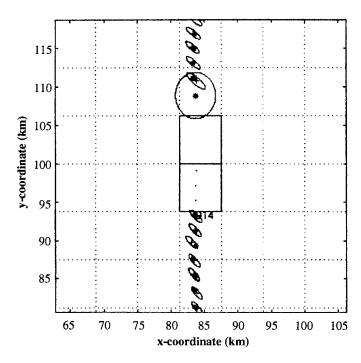


**Figure 2-4:** Compensated Tracker Response for Maneuvering Target. "Smile" Shaped Centripetal Gates used with (0.0-0.5) g Range of Across-Track Acceleration Allowance

#### 2.2.3 Shadow Rule:

The shadow rule provides a means of preserving firm tracks that enter regions shadowed from the radar line of sight. If the predicated track gate center falls within a designed shadow region, both the track state and gate size will be frozen. Upon emerging from the shadow, state promotion resumes and the gate size will not be allowed to exceed a maximum value. In the tracker scenario used in Figures 2-5 and 2-6, only a minimal amount of acceleration noise, 0.05 g units, was used in order to maintain a straight line coasting of the track through the shadow. As previously, the target has a speed of 250 meters per second and the update scan time is 10 seconds.

Figure 2-5 shows a section of tracker response, when no shadow rule is in effect, for a target approaching a shadow zone (shaded rectangle) from below. The three dots denote extrapolated positions of the initial track where no reports were captured. After four demotions the firm track that initially entered the shadow was dropped, as indicated by the D14 symbol. A new tentative track was spawned, and promoted, once the predicted gate positions moved beyond the shadow. Note that the D symbol has been placed at the last updated track position, just prior to entering the shadow, where the track was 14 scans old.



**Figure 2-5:** Tracker Response for Target Flying through Shadow No Shadow Rule Applied

Figure 2-6 shows the track history for the same target-shadow scenario when the shadow rule was in place. The circles in the shadow denote coasted track positions at which the track state was held fixed. Once the predicted gate position emerged from the shadow, there was a

moderate increase in gate size, after which it settled down, and the original firm track continued undisturbed.

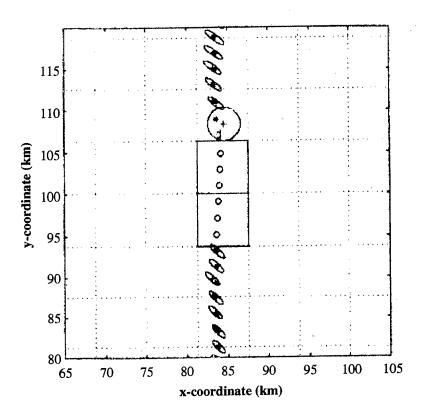


Figure 2-6: Tracker Response for Target Flying through Shadow Shadow Rule Applied

#### 2.2.4 Discrete Rule:

By tagging large radar returns, or discretes, the STAP processor can exclude regions containing them from its covariance matrix element formation and thereby not use up limited degrees of freedom on their cancellation. The discrete rule allows the tracker to coast through any region containing one of these tagged returns and to essentially ignore it. If a known discrete falls within a track gate, that track will be treated as if in a shadow and will not be updated.

In Figure 2-7, the same target speed, update time, and acceleration noise have been used as in the shadow rule examples. A discrete has been inserted in the target trajectory as shown. As indicated, the tracker preserves the state value of 4 as the predicted gate positions passes through the discrete.

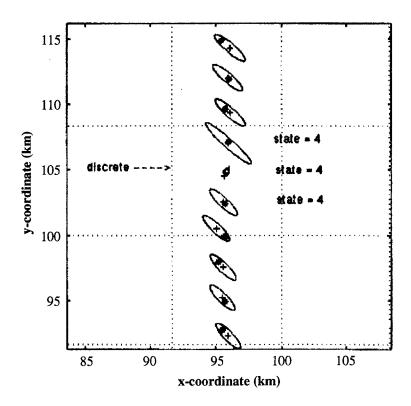


Figure 2-7: Tracker Response for Target Passing Near a Discrete Discrete Rule Applied

The previous discussion looked at the implementation of four specific tracking rules. However, many more rules that were considered relevant to the STAP problem were developed during the course of this tracking study. In addition to the rule topics discussed here, issues regarding the assignment of target priority, detection threshold, state promotion logic, and other features were considered. A collection of twenty-five such rules are presented in the "Knowledge-Based Tracker Rule Book" that is included in Volume V of this report. Included with each rule is a discussion of its rationale, its impact on the overall knowledge based system and interface requirements that might exist between the tracker, controller and radar.

### 3.0 Software Description

All tracking software used in this effort has been written in Matlab 5.1. A total of 49 modules are listed and documented below. These can be subdivided into three groupings consisting of user interface, main tracker, and tracker utilities. The first two modules belong to the user interface group. These are Tracker\_GUI\_7, which provides the graphical user interface for the overall tracking simulation, and Setup\_Tracker\_6, which sets up the interface between the tracker and the scenario generator. The main tracker group contains the multiple target tracking module, Run\_Tracker\_8, which carries out all prediction, smoothing, and association operations on report data on a per scan basis. Finally, the tracker utilities group contains all of the support modules that are used by the tracker. It should be noted that some of the modules supporting the user interface group have not been documented since that portion of the software is going to be removed by the customer and replaced with their own hooks into the STAP simulation software.

#### **User Interface Modules**

Tracker\_GUI\_7 Setup\_Tracker\_6

Main Tracker Module Run\_Tracker\_8

**Tracker Utility Modules** 

put\_Table\_R\_2

get\_Table\_R\_2

put\_Table\_Trk\_4

get\_Table\_Trk\_4

add\_Table\_Trk\_4

Cleanup\_Table\_Trk

print\_Table\_Trk

Display\_Trk\_Data\_5

State\_Update

set\_Trackstate

set\_TrackHM\_stat

set\_Track\_gates

Shadow\_Updates

set\_Track\_Shadow

predict\_shlx\_x

Kal\_b\_pred

Kal\_c\_pred

smooth\_shlx

Kal\_b\_smth

Kal\_c\_smth

first\_smooth\_shlx

abtrack\_init

track\_init\_2

Tracker\_GUI\_7

Calling Module:

None

Called Modules:

All\_Defaults\_4
Demo\_Defaults\_4
Read\_Scenario\_2
Write\_Scenario\_2
Track\_Data\_Gen\_4
Radar\_menu\_3
Tracker\_Opt\_menu\_2
Setup\_Tracker\_6

Setup\_Tracker\_6
Run\_Tracker\_8

Inputs:

None

Outputs:

None

Globals:

\*\*\*\*Radar\_menu\_3\*\*\*

first\_in\_Radar

f\_Ghz N\_hits SNR0\_dB Prf\_kHz DRng\_m Az\_mrad\_3dB Dop\_hz

Pfa SNR\_fa\_dB

\*\*\*Scenario\_menu\*\*\*

script\_name

Tracker\_Opt\_resp

\*\*\*Track\_Filter\_menu\*\*\*

Tfilt\_resp

\*\*\*Tracker\_param\_menu\*\*\*

first\_in\_Tr\_parm

Tfilt\_resp

Mult\_LP Mult\_HP radius\_TENT\_LP radius\_TENT\_HP

Man\_amt alpha beta Pri\_T

Turn\_int gate\_case

\*\*\*Tracker\_prom\_menu\*\*\*

first\_in\_Tr\_prom

Hit\_Tbl\_LP Miss\_Tbl\_LP Hit\_Tbl\_HP Miss\_Tbl\_HP

\*\*\* \*\*\*

fig\_no\_T

Time X-meas Y\_meas pDop\_meas report\_ID

X\_tru Y\_trum pDop\_tru S11 S12 S13 S22 S23 S33

Angle (radians) of prediction point ang\_pred Angle (radians) of track ang\_trk Draw track gate flag (1=> yes) gate\_on Print track gate flag (1=> yes) print\_Trk\_Tbl Label track with text (1=> yes) text\_on Number of shadow zones in scenario N\_shadow Array of low x shadow tile values x\_sh\_LO Array of high x shadow tile values x\_sh\_HI Array of low y shadow tile values y\_sh\_LO Array of high y shadow tile values y\_sh\_HI In shadow flag (1=> yes)In\_Shadow Number of consecutive dwells in shadow Nshadow\_dwells

#### Globals:

Mult Table\_R Table\_T

DROPPED TENT FIRM

LP HP

SUM1\_ERROR SUM2\_ERROR

P\_DET HP\_Buf dBuf

Display\_cnt

#### Description:

Initializes and sets up variables to be used by the Run\_Tracker\_8 program. Puts scenario generator outputs in a form usable by tracker. Also adds false alarms to scenario generation data.

Run\_Tracker\_8

Calling Modules:

None (script file)

Called Modules:

put\_Table\_R\_2 get\_Table\_R\_2 get\_Table\_Trk\_4 put Table Trk 4 add\_Table\_Trk\_4 predict\_shlx\_x first\_smooth\_shlx smooth\_shlx Get\_Semiaxes\_3 Test\_E\_Gate Test\_Smile\_Gate get\_def\_Cov\_manu Assign\_Cov\_manu State\_Update set\_Trackstate set\_TrackHM\_stat Pred\_Shadow\_Test Shadow\_Update Discrete\_Test set\_Track\_Shadow get\_track\_ang get\_pred\_ang update\_error TR\_Assoc\_Max\_T Display\_Trk\_Data\_5 print\_Table\_T Load\_dBuf\_4 plot\_dBuf Cleanup\_Table\_Trk

Inputs:

setup by Tracker\_GUI\_7 and

Setup\_Tracker\_6

Outputs:

None

Globals:

None

Description:

The multiple target tracker processes report data collected during each scan and performs three basic functions: track-report correlation, association, and maintenance.

put\_Table\_R\_2

Calling Module:

Run\_Tracker

Called Modules:

None

Inputs:

Time

Time of radar blips

X meas, Y\_meas

Measured position (km)

FDop\_meas

Measured pseudo Doppler (km\*km/sec)

X tru, Y\_tru

True position (km)

FDop\_tru

Truer pseudoDoppler (km\*km/sec)

S11, ..., S33

Measurement Covariance

sig\_Rng\_km

Range Measurement error (km)

sig\_Az\_rad sig\_Rdot\_kmps

Azimuth measurement error (radians) Range rate measurement error (km/sec)

freq\_GHz

Radio frequency of radar (gHz)

Det\_Level

Detection level

Prior\_intel

Priority status Maneuver status

Manu intel report\_ID

Trajectory ID of report

Nrep

Number of reports calling Module: Run\_Tracker

Called Modules:

None

Inputs:

Time

Time of radar blips (sec)

X\_meas, Y\_meas

Measured position (km)

FDop\_meas

Measured pseudo Doppler (km\*km/sec)

X\_tru, Y\_tru

True position (km)

FDop\_tru

True pseudoDoppler (km\*km/sec)

S11, ..., S33

Measurement Covariance

sig Rng\_km

Range Measurement error (km)

sig\_Az\_rad sig\_Rdot\_kmps Azimuth measurement error (radians) Range rate measurement error (km/sec)

freq\_GHz

Radio frequency of radar (gHz)

Det Level

Detection level Priority status

Prior\_intel Manu\_intel

Maneuver status

report\_ID

Trajectory ID of report

Nrep

Number of reports calling Module: Run\_Tracker

scan

Current scan index

Outputs:

Table\_R

Globals:

Table\_R

Description:

Load the report table buffer for the current scan. All arrays are indexed as (report, scan) and were created by a scenario generator.

get\_Table\_R\_2

Calling Module:

Run\_Tracker\_8

Called Modules:

None

Inputs:

rep

report index

#### Outputs:

 $T_m$ 

Blip time (sec)

X\_m, Y\_m

Measured position (km)

FDop\_m

Measured Doppler (km\*km/sec)

Cov\_m\_vec

Measured covariance vector

sig\_rng\_km\_m sig\_crng\_km\_m Range measurement error (km) Cross range measurement error (km)

sig\_Rdot\_kmps\_m

Range rate measurement error (km?sec)

freq\_GHz

Radar rf frequency (gHz)

Det\_m priority\_in Detection level Priority Status

maneuver\_in report\_source

Maneuver status Trajectory ID

X\_tru\_m, Y\_tru\_m

True position (km)

FDop\_tru\_m

True pseudoDoppler (km\*km/sec)

error\_status

not used

Globals:

Table\_R

#### Description:

Fetch report table data for current scan.

put\_Table\_Trk\_4

Calling Module:

Run\_Tracker\_8

Called Modules:

None

Inputs:

trk Track index
TID Track ID number

status (drop, tentative, firm)

state Track state (quality index;  $0 \Rightarrow dropped$ )

report Captured report index

scan1 Scan index when track became firm

trk\_type Tracker type (alpha beta, unc/extd Kalman)

Z\_m Measurement state vector

Cov\_m\_vec Measurement covariance vector

T\_m Measurement of time of captured report

priority Priority status of track
maneuver Maneuver status of track
Z\_p Prediction state vector
Cov\_p\_vec Prediction covariance vector

Z\_s Smoothed state vector

Cov\_s\_vec Smoothed covariance vector

HM\_flg Track capture flag  $(0 \Rightarrow miss, 1 + hit)$ 

ang\_trk Track angle (radians)
x\_s\_2LST Last track x position (km)
y\_s\_2LST Last track y position (km)
T\_s\_2LST Last track time (sec)

semi\_rng\_T along range semi axis (km)
semi\_crng\_T cross range semi axis (km)
semi\_trk\_T along track semi axis (km)
semi\_ctrk\_T cross track semi axis (km)
In-Shadow Shadow status flag (0 => not in)

gate\_case Track gating choice (0:3)

Accel\_max Maximum acceleration (km/sec\*sec)

sig\_rng\_km range measurement error (km)

sig\_crng\_km cross range measurement error (km) sig\_Rdot\_kmps2 range rate meas error (km\*km/sec)

#### Outputs:

error\_status
Table T

Globals:

Table\_T

Description:

Updates track table data for current scan and report index.

get\_Table\_Trk\_4

Calling Module:

Run\_Tracker\_8

Called Modules:

None

Inputs:

trk

Outputs:

same as inputs to put\_Table\_Trk\_4 same as inputs to put\_Table\_Trk\_4

TID

sig\_Rdot\_kmps2

Globals:

Table\_T

Description:

Fetch track table data for current scan and report index.

add\_Table\_Trk\_4

Calling Module:

Run\_Tracker\_8

Called Modules:

None

Inputs:

Ntrk

num\_new\_trks

TID\_New

same as inputs to put\_Table\_Trk4

•

 $sig\_Rdot\_kmps2$ 

Outputs:

error\_status

Table\_T

Globals

Table\_T

Description:

Insert new tentative tracks into track table.

Cleanup\_Table\_Trk

Calling Module:

Run\_Tracker\_8

Called Modules:

None

Inputs:

None

Outputs:

Ntrk

Number of valid tracks

Globals:

Table\_T

Description:

Updates track table for next scan. Sorts Table\_T by column 3 (state) and removes all zero states. Counts number of remaining valid tracks and returns this value.

print\_Table\_T

Calling Module:

Run\_Tracker\_8

Called Modules:

None

Inputs:

Ntrk

Number of track sets to be printed (max = 10)

sup

vector of Table\_T indices to be printed

Outputs:

prints to command tool

Globals:

Table\_T

Description:

Prints track table information as columns (one per track). Support vector sup is subset of {1:86} corresponding to fields in Table\_T.

Display\_Trk\_Data\_5

Calling Module:

Run\_Tracker\_8

Called Modules:

Draw\_Grid

get\_Table\_Trk\_4
get\_Table\_R\_2
Assign\_Cov\_manu
predict\_shlx\_x
get\_sig\_track
get\_pred\_ang
E\_Gate\_Semiaxes
Draw\_Smile\_Gate
Draw\_E\_Gate\_2

Inputs:

Ntrk

Number of tracks to be plotted

scan scan\_period current scan index scan time (sec)

sig\_rng\_km\_nom

not used

sig\_Az\_rad\_nom

not used

plot\_vec

plot scale: (xmin, xmax, ymin, ymax)

x\_v, y\_v

x and y grid point sets x and y grid spacing

dx, dy gate\_on

Draw track gate flag  $(1 \Rightarrow yes)$ 

text\_on

Print Text gate plot figure number

fig\_no symbol\_1

rng-cross rng aligned gate symbol trk-cross trk aligned gate symbol

symbol\_2 semi-max

maximum gate size allowed

Outputs:

graphical display in figure (fig\_no)

Globals:

Display\_cnt

Table R Table T

DROPPED TENT FIRM LP HP

Mult\_LP Mult\_HP radius\_TENT\_LP radius\_TENT\_HP

sig\_trk\_km sig\_ctrk\_km gate\_case

Cov\_man20 Cov\_man30 Cov\_man\_acc\_x Cov\_man\_acc\_y

#### Description:

The module serves as a diagnostic and display tool for the multi target tracker. It displays predicted and measured positions prior to track table cleanup and draws track gates centered on predicted positions.

set\_Trackstate

Calling Module:

Run\_Tracker\_8

Called Modules:

None

Inputs:

state trk

Outputs:

None

Globals:

 $Table\_T$ 

Description:

Inputs state value into track table at index trk.

set\_TrackHM\_stat

Calling Module:

Run\_Tracker\_8

Called Modules:

None

Inputs:

HM\_flg

Capture/shadow status of track

trk

Track index

Outputs:

None

Globals:

Table\_T

Description:

Inputs the track capture/shadow status into track table.

set\_Track\_gates

Calling Module:

Run\_Tracker\_8

Called Modules:

None

Inputs:

semi\_rng\_T

Along range semi axis of ellipse gate

semi\_crng\_T semi\_trk\_T Cross range semi axis Along track semi axis

semi\_trk\_T
semi\_ctrk\_T

Along track semi axis Cross track semi axis

trk

Track table index

Outputs:

None

Globals:

Table\_T

Description:

Inputs ellipse gate semi axes into track table corresponding to index trk.

Shadow\_Update

Calling Module:

Run\_Tracker\_8

Called Modules:

set\_Track\_Shadow set\_TrackHM\_stat

Inputs:

trk

Track index into Table\_T

In\_Shadow

Shadow status flag  $(1 \Rightarrow \text{in shadow})$ 

Nshadow\_dwells\_last Number of scans input trk in shadow

HM\_flg\_last

Capture/shadow status of input trk

Outputs:

None

Globals:

Table\_T

Description:

Updates track shadow status corresponding to index trk. If track is in a shadow, the number of shadow dwells is incremented and the capture status is set to the number 2. Otherwise, the number of dwells is et to zero and the capture status maintained.

set\_Track\_Shadow

Calling Module:

Run\_Tracker\_8 Shadow\_Update

Called Modules:

trk

None

Inputs:

Nshadow\_dwells

Number of consecutive dwells in shadow

In\_Shadow

in shadow status flag Index into Table\_T

Outputs:

None

Globals:

Table\_T

Description:

Inputs shadow parameters into track table corresponding to index trk. These include (1) the # of consecutive dwells of track in a shadow, and (2) the in-shadow status flag (0 => not in shadow,  $1 \Rightarrow$  in shadow).

predict\_shlx\_x

Calling Module:

Run\_Tracker\_8

Called Modules:

Kal\_b\_pred Kal\_c\_pred

Inputs:

type

Tracking filter type (1:3 +. alpha beta, uncoupled Kalman, and

extended Kalman)

Z s last

Smoothed state vector at last scan

Cov\_s\_last\_vec

Smoothed covariance array at last scan

Cov\_man\_x
Cov\_man\_y

Maneuver covariance matrix of x component Maneuver covariance matrix of y component

Cov\_man

Maneuver covariance matrix of extended Kal

dΤ

Time interval from last update to present

Outputs:

Z-P

Prediction state vector

Cov\_p\_vec

Prediction covariance matrix

Globals:

None

#### Description:

Computes predicted state vector and Covariance array, Z\_p and Cov\_p\_vec, respectively. The method used depends on the tracking filter type specified. The maneuver covariance matrices provide a means for inputting acceleration noise to increase track gate size for the Kalman filter cases

### **Equations:**

alpha beta:

 $X_p = x_s + vx_s + dT$ 

 $Y_p = y_s_{last} + vy_s_{last} * dT$ 

 $Vx_p = vx_s_{last}$ 

 $Vy_p = vy_s_{last}$ 

where the components X\_p, Vx\_p, etc., are related to the state vectors Z\_p, Z\_s\_last, etc. by stacking the x and y components of position, velocity, and acceleration

Z=[X;Vx;Ax;Y;Vy;Ay]

Uncoupled Kalman: see Kal\_b\_pred

Extended Kalman:

see Kal\_c\_pred

Kal\_b\_pred

Calling Module:

predict\_shlx\_x

Called Modules:

None

Inputs:

Z\_s\_in

3 x 1 Smoothed input state vector (either component)

[Position; Velocity; Acceleration]

dt\_in

Time since last update

Cov\_manu

3 x 3 Covariance matrix of maneuver noise

Cov\_s\_in

3 x 3 Smoothed input covariance matrix (either component)

[Position; Velocity; Acceleration]

Outputs:

Z\_p\_out

3 x 1 Prediction state vector (corresponding component)

Cov\_p

3 x 3 Prediction covariance matrix

Globals:

Table\_T

### Description:

Computes 3 x 1 prediction state vector and 3 x 3 prediction covariance matrix for the case of an uncoupled Kalman filter. All input and output state vectors are assumed to be 3 x 1, and all covariance matrices are 3 x 3.

### Equations:

$$\phi = \begin{bmatrix} 1 & dT & 0.5(dT)^2 \\ 0 & 1 & dT \\ 0 & 0 & 1 \end{bmatrix}; 3 \times 3 \text{ state transition matrix}$$

$$Z_p_out=\phi*Z_s_in$$

 $(\phi'$  denotes the transpose of  $\phi)$ 

Kal\_c\_pred

Calling Modules:

predict\_shlx\_x

Called Modules:

None

Inputs:

Z_s_in	4 x 1	Smoothed input state vector
		[X_s_in; Vx_s_in; Vy_s_in]
dt_in		Time since last update
Cov_manu	4 x 4	Covariance matrix of maneuver noise
Cov_s_in	4 x 4	Smoothed input covariance matrix

## Outputs:

Z_p_out	4 x 1	Prediction state vector
		[X_p_out; Vx_p_out; Y_p_out; Vy_p_out
Cov_p	4 x 4	Prediction covariance matrix

Globals:

None

## Description:

Computes  $4 \times 1$  prediction state vector and  $4 \times 4$  prediction covariance matrix for the case of an extended Kalman filter. All input and output state vectors are assumed to be  $4 \times 1$ , and all covariance matrices are  $4 \times 4$ .

# Equations:

$$\phi = \begin{bmatrix} 1 & dT & 0 & 0 \\ 0 & 1 & 0 & 0 \\ 0 & 0 & 1 & dT \\ 0 & 0 & 0 & 1 \end{bmatrix}; 4 \times 4 \text{ state transition matrix}$$

$$Z_p_out = \phi * Z_s_in$$
  
 $Cov_p = \phi * Cov_s_in * \phi' + Cov_man$ 

( $\phi$ ' denotes the transpose of  $\phi$ )

smooth\_shlx

Calling Module:

Run\_Tracker\_8

Called Modules:

Kal\_b\_smth Kal\_c\_smth

Inputs:

type

Tracking filter type (1:3 => alpha beta, uncoupled Kalman, and

extended Kalman)

 $Z_m$ 

Measurement vector (x;y;pDop)

 $Z_p$ 

Prediction state vector (X;Vx;Ax;Y;Vy;Ay)

Cov\_p\_vec

Prediction cov array (Cov\_p\_x;Cov\_p\_y)reshaped to 1 x 18

Cov\_m\_vec

Meas cov array 1 x 9

dT

Time interval from last update to present

Outputs:

 $Z_s$ 

Smoothed state vector (X;Vx;Ax;Y;Vy;Ay)

Cov\_s\_vec

Smoothed cov array (Cov\_s\_x;Cov\_s\_y)reshaped to 1 x 18

Gain\_mat

Gain matrix (not used by tracker)

Globals:

alpha beta

#### Description:

Computes smoothed state vector and Covariance array, Z\_s and Cov\_s\_vec, respectively. Also returns a gain matrix (not normally used) which can be used for diagnostic purposes. The smoothing method used depends on the tracking filter type specified.

# Equations:

alpha beta:

 $Dx = x_m - X_p$ 

 $x_s = X_p + alpha * Dx$ 

 $Vx_s = Vx_p + beta * Dx/dT$ 

 $Dy = y_m - Y_p$ 

 $y_s = Y_p + alpha * Dy$ 

 $Vy_s = Vy_p + beta * Dy/dT$ 

where

 $Z_m = [x_m; y_m; pDop_m)$ 

and Z\_p and Z\_s are 6 x 1 vectors of the position, velocity and acceleration components

Uncoupled Kalman:

see Kal\_b\_smth

Extended Kalman:

see Kal\_c\_smth

Kal\_b\_smth

Calling Module:

smooth\_shlx

Called Modules:

None

Inputs:

Z_m	3 x 1	Measurement vector [x_m;y_m;pDop_m]
	2 1	Tricusarement vector [x_m,y_m,pDop_m]
Z_p_out	3 x 1	Prediction state vector (either component)
		[Position; Velocity; Acceleration]
Cov_p	3 x 3	Covariance matrix of maneuver noise
Cov_s_in		Prediction covariance matrix
var meas		Measurement variance

Outputs:

Z_s_out	3 x 1	Smoothed output state vector (either component) [Position; Velocity; Acceleration]
Cov_s_out Res dist_Res_2 S	3 x 1	Smoothed output covariance matrix Residual error vector (Innovations) Statistical distance Gain matrix

Globals:

None

### Description:

Computes 3 x 1 smoothed state vector and 3 x 3 smoothed covariance matrix for the case of an uncoupled Kalman filter. All input and output prediction and smoothed state vectors are assumed to be  $3 \times 1$ , and all covariance matrices are  $3 \times 3$ .

## Equations:

```
(for either x or y component)

M = [1 0 0]; Measurement Matrix (1 Measurement x 3 states)

I_Cov_Res = 1/(M * Cov_p * M' + var_meas)

S = Cov_p * M' * I_Cov_Res; Gain Matrix (3 states x 1 measurement)

Z_s_out = Z_p_out + S * (Z_m - M * Z_p_out)

Cov_s_out = (I - S * M) * Cov_p

Res = (Z_m - M * Z_p); Innovations

dist_Res_2 = Res * I_Cov_Res * Res'; Statistical distance
```

Kal\_c\_smth

Calling Modules:

smooth\_shlx

Called Modules:

None

Inputs:

Z_m	3 x 1	Measurement vector (3 x 1) [x_m;y_m;pDop_m]
Z_p_out	4 x 1	Prediction state vector [X; Vx; Y; Vy]
Cov_p	4 x 4	Prediction covariance matrix
Cov_meas	3 x 3	Measurement Covariance

### Outputs:

Z_s_out	4 x 1	Smoothed output state vector [X; Vx; Y; Vy]
Cov_s_out	4 x 4	Smoothed output covariance matrix
Res	3 x 1	Residual error vector (Innovations)
dist_Res_2		Statistical distance
S	4 x 3	Gain Matrix

Globals:

None

### Description:

Computes  $4 \times 1$  smoothed state vector and  $4 \times 4$  smoothed covariance matrix for the case of an extended Kalman filter. All input and output prediction and smoothed state vectors are assumed to be  $4 \times 1$ , and all covariance matrices are  $4 \times 4$ .

## Equations:

$$M = \begin{bmatrix} 1 & 0 & 0 & 0 \\ 0 & 0 & 1 & 0 \\ M_{31} & M_{32} & M_{33} & M_{34} \end{bmatrix}; \text{Measurement matrix (3 Measurements x 4 states)}$$

where

$$M_{31} = 0.5 * Z_p_out (2)$$

$$M_{32} = 0.5 * Z_p_out (1)$$

$$M_{33} = 0.5 * Z_p_out (4)$$

$$M_{34} = 0.5 * Z_p_out (3)$$

## Note that

$$\begin{array}{l} (pDop)_{est} = M_{31} * X_p + M_{32} * Vx_p + M_{33} * Y_p + M_{34} * Vy_p \\ \\ I\_Cov\_Res = (M * Cov_p * M' + Cov\_meas) - 1 \\ S = Cov\_p * M' * I\_Cov\_Res ; 4 x 3 Gain Matrix (4 states x 3 measurements) \\ Res = (Z_m - M * Z_p\_out) ; 3 x 1 Innovations \\ Z\_s\_out = Z_p\_out + S * Res 4 x 1 \\ Cov\_s\_out = (I - S * M) * Cov\_p 4 x 4 \\ dist\_Res\_2 = Res; * (I\_Cov\_Res) * Res \\ \end{array}$$

first\_smooth\_shlx

Calling Module:

Run\_Tracker\_8

Called Modules:

abtrack\_init\_track\_init\_2track\_init\_c

Inputs:

type

Track filter type (1:3 => alpha beta, Uncoupled Kalman, and

extended Kalman

Z\_m\_last

Measured vector (last update) Measured vector (current)

Z\_m Cov\_m\_vec

Meas Covariance array (current)

ďΤ

Time interval (sec) from last update

Outputs:

Z\_s\_out

Smoothed state vector

Cov\_s\_vec

Smoothed covariance array

Globals:

None

Description:

Performs smoothing of tentative tracks

Equations:

alpha beta:

see abtrack\_init

Uncoupled Kalman:

see track\_init\_2

Extended Kalman:

see track\_init\_c

abtrack\_init

Calling Module:

first\_smooth\_shlx

Called Modules:

None

Inputs:

(x1,y1) (x2, y2)

Last updated track position

Current track position

dT12 Time interval (sec)

Outputs:

(x\_s, y\_s) (vx\_s, vy\_s) ang\_trk

Smoothed track position Smoothed tracked velocity

Track angle (radians)

Globals:

None

Description:

Does a two point initialization of an alpha beta tracker using current and last track positions and their time interval.

Equations:

Dx = (x2 - x1)

 $x_s = x^2$ 

 $vx_s = Dx/dT12$ 

 $D\dot{y} = (y2 - y1)$ 

 $y_s = y_2$ 

 $vy_s = Dy/dT12$ 

 $ang_{trk} = arctan (Dy/Dx)$ 

track\_init\_2

Calling Module:

first\_smooth\_shlx

Called Modules:

None

Inputs:

Delt

Time (sec) between current and last update

z\_pos\_1

Last position component update (x or y)

z\_pos\_2

Current position component (x or y)

var\_pos\_m\_2

Measurement variance of position component

Outputs:

 $Z_s_{in}$ 

Smoothed state vector  $(3 \times 1)$ 

P\_s\_in

Smoothed covariance matrix (3 x 3)

Globals:

None

Description:

Does a two point initialization of an uncoupled Kalman tracker. This routine is applied separately to both the x and y components of target motion.

Equations:

$$Z_s_{in} = [pos_s; vel_s; 0]$$

$$P_{s_{12}} = \begin{bmatrix} Px_{11} & Px_{12} & 0 \\ Px_{12} & Px_{22} & 0 \\ 0 & 0 & 0 \end{bmatrix}$$

where

$$Px_{11} = var_pos_m_2$$

$$Px_{12} = Px_{11}/Delt$$

$$Px_{22} - Px_{11}/(Delt)2$$

track\_init\_c

Calling Module:

first\_smooth\_shlx

Called Modules:

sig\_xy

None

Inputs:

Delt Time (sec) between current and last update Last position update (x1, y1)(x2, Y2)Current position Measurement covariance xx comp sig\_xx Measurement covariance yy comp sig\_yy Measurement covariance xy comp

Outputs:

 $Z_s_{in}$ 4 x 1 Smoothed state vector P s in 4 x 4 Smoothed covariance matrix

Globals:

None

Description:

Does a two point initialization to be used with the extended Kalman track filter.

Equations:

Let T = Delt, T2 = T<sup>2</sup>  

$$sig_x = \sqrt{sig_xx}$$
,  $sig_y = \sqrt{sig_yy}$ 

 $pos_sx = x2$ ,  $pos_sy = y2$ ; smoothed positions  $vel_sx = (x2 - x1)/T$ ,  $vel_sy = (y2 - y1)/T$ ; smoothed velocities  $Z_s_{in} = [pos_sx; vel_sx; pos_sy; vel_sy]$ 

$$P\_s\_in = \begin{matrix} P_{11} & P_{12} & P_{13} & P_{14} \\ P_{12} & P_{22} & P_{23} & P_{24} \\ P_{13} & P_{23} & P_{33} & P_{34} \\ P_{14} & P_{24} & P_{34} & P_{44} \end{matrix}$$

where

$$P_{11} = sig_xx$$
,  $P_{12} = 1.5 * P_{11}/T$ ,  $P_{13} = sig_xy$ ;  $P_{14} = 1.5 * sig_x * sig_y/T$ .  $P_{22} = 6.5 P_{11}/T2$ ;  $P_{23} = P_{14}$ ,  $P_{24} = sig_xy/T2$ .  $P_{33} = sig_yy$ ,  $P_{34} = 1.5 * P_{33}/T$ .  $P_{44} = 6.5 * P_{33}/T2$ 

Assign\_Cov\_manu

Calling Module:

Run\_Tracker\_8

Called Modules:

get\_def\_Cov\_manu

Inputs:

trk\_type

Track filter type

scan

Current scan

manu\_rep

Maneuver anticipation status flag

rep\_source

Maneuver anticipation interval (scan lo, scan hi)

Outputs:

Cov\_man

Maneuver covariance matrix

Cov\_man\_x Cov\_man\_y

Globals:

Cov\_man20

 $Cov\_man30$ 

Cov\_man\_acc\_x

Cov\_man\_acc\_y

Turn\_int

Description:

Sets up the maneuver covariance matrix. If a maneuver has been anticipated for the current scan then maneuver noise is applied. Otherwise a small value (essentially zero) is loaded into the matrix.

Equations:

Accel\_max = Maximum maneuver acceleration (km/s<sup>2</sup>)

 $var\_acc = (Accel\_max)^2$ 

 $var_vel = (Accel_max * scan_period)^2$ 

 $var_pos = (0.5 * Accel_max * (scan_period)^2)^2$ 

 $Cov_man = \begin{bmatrix} \mathbf{var} & pos & 0 & 0 \\ 0 & \mathbf{var} & vel & 0 \\ 0 & 0 & \mathbf{var} & acc \end{bmatrix}; trk_type \neq 3$ 

$$Cov_man = \begin{bmatrix} \mathbf{var}_pos & 0 & 0 & 0 \\ 0 & \mathbf{var}_vel & 0 & 0 \\ 0 & 0 & \mathbf{var}_pos & 0 \\ 0 & 0 & 0 & \mathbf{var}_vel \end{bmatrix}; trk_type = 3$$

$$Cov_man_x = Cov_man_y = Cov_man$$

get\_def\_Cov\_manu

Calling Module:

Assign\_Cov\_manu

Called Modules:

None

Inputs:

trk\_type

Track filter type

Outputs:

Cov\_man

Maneuver covariance matrix

Cov\_man\_x

Cov\_man\_y

Globals:

Cov\_man20

Cov\_man30

Description:

Loads default values into maneuver covariance matrices.

Equations:

Cov\_man = Cov\_man20;

trk\_type ≠ 3

Cov\_man = Cov\_man30;

 $trk\_type = 3$ 

Cov\_man\_x = Cov\_man\_y = Cov\_man;

where

 $Cov_{man20} = le-10 * eye (3)$ 

 $Cov_{man 30} = le-6 * eye (4)$ 

Get\_Semiaxes\_3

Calling Module:

Run\_Tracker\_8

Called Modules:

E Gate Semiaxes 3

get\_sig\_track

Scale\_Shadow\_gates

Inputs:

In\_Shadow

Current in shadow flag  $(1 \Rightarrow yes)$ 

In\_Shadow\_last

Last update in shadow flag

Nshadow\_dwells\_last Number of successive dwells in shadow as of last update

gate\_case

Gate type flag (0:3) Track filter type (1:3)

trk\_type

Gate size multiplier

Mult Accel max

Maximum assumed acceleration

dT

Time (sec) since last update

ang\_pred

Angle (rad) of predicted point wrt radar cs

ang\_trk
sig\_rng\_km\_m

Angle (rad) of track wrt radar cs Range measurement error (km)

sig\_crng\_km\_m
Z\_s\_last

Cross range measurement error (km) Smoothed state vector (last update)

Z\_p

Prediction state vector (current)

Cov\_p\_vec semi-rng\_T\_last

prediction covariance array (current) Along range semi axes (last)

semi\_crng\_T\_last

Cross range semi axes (last)

semi\_trk\_T\_last

Along track semi axes (last) Cross track semi axes (last)

semi\_ctrk\_T\_last semi\_max

Maximum allowed semi axis size

Outputs:

semi\_rng\_T

Along range semi axes (current)

semi\_crng\_T semi\_trk\_T Cross range semi axes (current) Along track semi axes (current)

semi\_ctrk\_T

Cross track semi axes (current)

Globals:

None

#### Description:

Computes the semi axes for the two orientations of elliptical gates used. The first type is oriented along and across range and the second is oriented along and across track. Tracks that are in a shadow have their gate sizes frozen. Otherwise, track gates sizes are determined as a function of the gate case and track filter type selected. This function is done by the routine E\_Gate\_Semiaxes\_3.

E\_Gate\_Semiaxes\_3

Calling Module:

Get\_Semiaxes\_3

Called Modules:

Rotate\_xy2xpyp

Inputs:

gate\_case Gate type flag (0:3)
trk\_type Track filter type (1:3)
Mult Gate size multiplier

Z\_p Prediction state vector (current)
Cov\_p\_vec prediction covariance array (current)
Angle (rad) of predicted point wrt radar cs

sig\_rng
sig\_crng
Range measurement error (km)
sig\_crng
cross range measurement error (km)
ang\_trk
sig\_trk
sig\_ctrk
Along track measurement error (km)
sig\_ctrk
Cross track measurement error (km)

semi\_max Maximum allowed semi axes size

Outputs:

semi\_rng Along range semi axes (km)
semi\_crng Cross range semi axes (km)
semi\_trk Along track semi axes (km)
semi\_ctrk Cross track semi axes (km)

Globals:

None

#### Description:

Computes semi axes for elliptical gates oriented along/cross range, and oriented along/cross track. Results depend on which of three gate cases are chosen (cases 1 and 2 require a Kalman filter). In each case the along/cross track gate sizes are computed as scaled versions of the along/cross track measurement errors. However, the along/cross range oriented gate sizes are case dependent. Gate case 1 combines in an rss fashion (1) range and cross range measurement errors from the last track update, and, (2) current prediction covariance estimates in x and y, projected onto the range/cross range axes. The composite gate is formed by multiplying this result by a scale factor. Gate case 2 uses only the scaled prediction covariance estimates in x and y to form the gate. Gate case 3 uses the scaled along/cross range measurement errors to form this gate.

### Equations:

The quantities sig\_rng and sig\_crng are measurement errors along range and cross range computed from the last report captured by a given track and stored in the track table. The quantities sig\_trk and sig\_ctrk are based on kinematical assumptions and are computed in get\_sig\_track.

alpha beta filter:

### Kalman filters:

Get prediction uncertainty along x and y directions ( $\sigma_{px}$ ,  $\sigma_{py}$ ) from the covariance array Cov\_p\_vec.

 $(gate\_case = 1)$ 

 $\Delta\theta = (ang\_pred - ang\_trk)$ 

Compute projections of  $\sigma_{px}$  and  $\sigma_{py}$  onto the range-cross range axes.

$$\begin{bmatrix} \sigma_{px'} \\ \sigma_{py'} \end{bmatrix} = \begin{bmatrix} \cos(\Delta\theta) & \sin(\Delta\theta) \\ -\sin(\Delta\theta) & \cos(\Delta\theta) \end{bmatrix} \begin{bmatrix} \sigma_{px} \\ \sigma_{py} \end{bmatrix}$$

Form the "root sum square" (Rss) of  $\sigma_{px}$  and  $\sigma_{py}$  with the measurement errors

semi\_rng = Mult \* 
$$\sqrt{(\sigma px')^2 + (\text{sig\_rng})^2}$$
  
semi\_crng = Mult \*  $\sqrt{(\sigma px')^2 + (\text{sig\_crng})^2}$   
semi\_trk = Mult \* sig\_trk  
semi\_ctrk = Mult \* sig\_ctrk  
(gate\_case = 2)  
 $\theta$  = ang\_trk

Compute projections of  $\sigma_{px}$  and  $\sigma_{py}$  onto track-cross track axes.

$$\begin{bmatrix} \sigma_{px''} \\ \sigma_{y''} \end{bmatrix} = \begin{bmatrix} \cos(\theta) & \sin(\theta) \\ -\sin(\theta) & \cos(\theta) \end{bmatrix} \begin{bmatrix} \sigma_{px} \\ \sigma_{py} \end{bmatrix}$$

$$\begin{bmatrix} semi\_rng \\ semi\_crng \\ semi\_trk \\ semi\_ctrk \end{bmatrix} = Mult * \begin{bmatrix} sig\_rng \\ sig\_crng \\ |\sigma_{px''}| \\ |\sigma_{py''}| \end{bmatrix}$$

$$(gate\_case = 3)$$

get\_sig\_track

Calling Module:

Get\_Semiaxes\_3

Called Modules:

None

Inputs:

 $Z_s$ 

Smoothed state vector

Accel\_max

Maximum allowed acceleration (km/s\*s)

dΤ

Time (sec) since last update

Outputs:

sig\_trk\_km

Along track uncertainty (km)

sig\_ctrk\_km

Cross track uncertainty (km)

Globals:

None

Description:

Computes along/cross track uncertainties. The along track uncertainty is computed as  $0.5*A*(dT)^2$  with the along track acceleration A assumed bounded by 0.5g. The across track uncertainty is assumed to be due to constant speed turning only.

## Equations:

Define the following quantities:

Acc\_at = along track acceleration ≤ Accel\_max

V\_kmps = estimated track speed

 $\rho_{km}$  = radius of curvature of turn (km)

Ang = angle of turn voer time dT (radians)

 $\rho_{km} = (V_kmps)^2/Accel_max$ 

ang =  $V_kmps * dT/\rho_{km}$ 

 $sig_{trk}km = 0.5 Acc_{at} (dT)^{2}$ 

 $sig\_ctrk\_km = \rho_{km} (1 - cos (Ang))$ 

Scale\_Shadow\_Gates

Calling Module:

Get\_Semiaxes\_3

Called Modules:

None

Inputs:

gate\_scale semi-rng\_T\_in Gate size multiplier

semi\_crng\_T\_in semi\_trk\_T\_in semi\_ctrk\_T\_in Along range semi axis (input) Cross range semi axis (input) Along track semi axis (input) Cross track semi axis (input)

Outputs:

semi\_rng\_T\_out semi\_crng\_T\_out semi\_trk\_T\_out semi\_ctrk\_T\_out Along range semi axis (output) Cross range semi axis (output) Along track semi axis (output) Cross track semi axis (output)

Globals:

None

Description:

Multiplies input gate semi axes by a scale factor.

Rotate\_xy2xpyp

Calling Module:

E\_Gate\_Semiaxes\_3

Called Modules:

None

Inputs:

 $ang\_rad$ 

Rotation angle (rad)

 $\boldsymbol{Z}$ 

Input two component vector

Outputs:

Rotated two component vector

Globals:

None

Description:

Rotates the two component vector Z through angle ang\_rad.

Equations:

 $\theta = ang\_rad$  and

Let Rot =  $\begin{bmatrix} \cos(\theta) & \sin(\theta) \\ -\sin(\theta) & \cos(\theta) \end{bmatrix}$ 

 $Z_p = Rot * Z$ 

Test E\_Gate

Calling Module:

Run\_Tracker\_8

Called Modules:

Rotate\_xy2xpyp

Inputs:

 $Z_m$ 

Measurement state vector (x;y;pDop)

 $Z_p$ 

Prediction state vector (x;vx;ax;y;vy;ay)

ang\_rotn

Rotation angle wrt radar cs (radians)

semi\_along semi\_across Semi axis length along rotated x Semi axis length along rotated y

Outputs:

In E Gate

Inclusion test flag (1 => inclusion)

Globals:

None

Description:

Tests if measured point Z<sub>m</sub> lies within an ellipse which is (1) oriented at an angle "ang\_rotn" with respect to the radar coordinate system, (2) centered on the predicted position, Z<sub>p</sub>, and, (3) has semi axes of length semi\_along and semi\_across. Returns a value of zero if test fails, and a value of one if test passes.

### **Equations:**

Let  $(X_m, Y_m)$  and  $(X_p, Y_p)$  denote the measured predicted points, respectively. Transform the predicted-measurement position error into the local coordinate system of the ellipse, centered on the predicted point. The transformed residual errors  $(\Delta X', \Delta Y')$  are

$$\begin{bmatrix} \Delta X' \\ \Delta Y' \end{bmatrix} = \text{Rot } * \begin{bmatrix} X_p - X_m \\ Y_p - Y_m \end{bmatrix}$$

where

$$Y_e = semi\_across * \sqrt{1 - (\Delta X' / semi\_along)^2}$$

The condition for inclusion of (X<sub>m</sub>, Y<sub>m</sub>) within the ellipse is

$$|\Delta Y'| \le Y_e$$
 and

$$|\Delta X'| \le \text{semi\_along}$$

Test\_Smile\_Gate

Calling Module:

Run\_Tracker\_8

Called Modules:

None

Inputs:

 $T_s$ 

Scan period (sec)

 $Z_m$ 

Measurement state vector (x;y;pDop)

 $Z_p$ 

Prediction state vector (x;vx;ax;y;vy;ay) Smoothed state vector (last update)

Z\_s\_last x\_last\_km

x position (last update)

y\_last\_km

y position (last update)

ag\_HI

Maximum turn acceleration (g units)

semi\_rng

Measurement ellipse semi axis along range

semi\_crng

Measurement ellipse semi axis cross range

Outputs:

In\_gate\_m

Inclusion test flag  $(1 \Rightarrow included)$ 

Globals:

None

Description:

Tests if measurement ellipse intersects centripetal maneuver "smile" shaped gate.

# Equations:

The smile gate envelope is defined by two equations that are parameterized by the time t, ranging from the current report time to one scan period later. Let v denote the constant target speed and  $\rho$  be the radius of curvature of the turn. Then

$$\rho = v^2/(9.8 * ag_HI)$$
 and  
Ang = v (T\_s - t)/ $\rho$ .

With these the equations for the maneuver envelope in the local track coordinate system, centered on the last smoothed position, are

$$x'_s = vt + \rho \sin(ang)$$
  
 $y'_s = \rho(1 - \cos(ang))$ 

The gate test is performed by:

(1) Transforming the boundary points  $(x'_s, y'_s)$  to the radar coordinate system

$$\begin{bmatrix} x_s \\ y_s \end{bmatrix} = \begin{bmatrix} x_{last\_km} \\ y_{last\_km} \end{bmatrix} + \begin{bmatrix} \cos(\theta_{trk}) & -\sin(\theta_{trk}) \\ \sin(\theta_{trk}) & \cos(\theta_{trk}) \end{bmatrix} \begin{bmatrix} x_s' \\ y_s' \end{bmatrix}$$

where  $\theta_{trk}$  denotes the instantaneous track angle.

(2) Transforming  $(x_s, y_s)$  to local coordinate system centered on the measured point and oriented at the angle of the measured point  $\theta_m$ .

$$\begin{bmatrix} \Delta X_s'' \\ \Delta Y_s'' \end{bmatrix} = \begin{bmatrix} \cos \theta_m & \sin \theta_m \\ -\sin \theta_m & \cos(\theta_m) \end{bmatrix} \begin{bmatrix} x_s - x_m \\ y_s - y_m \end{bmatrix}$$

(3) Test each maneuver envelope point for inclusion within the measurement ellipse

$$|\Delta X_s''| \le \text{semi\_rng}$$
  
 $|\Delta Y_s''| \le Y_e$   
 $Y_e = \text{semi\_crng} \sqrt{1 - (\Delta X_s'' / \text{semi\_rng})^2}$ 

Pred\_Shadow\_Test

Calling Module:

Run\_Tracker\_8

Called Modules:

get\_def\_Cov\_manu predict\_shlx\_x Test\_In\_Shadow

Inputs:

trk\_type

Type of tracking filter (1:3)

Z\_s\_last

Smoothed state vector (last update)

Cov\_s\_last\_vec

Smoothed covariance array (last update)

dT

Time interval (sec) since last update

Outputs:

 $Z_p$ 

Prediction state vector

In\_Shadow

Shadow status flag  $(1 \Rightarrow \text{in shadow})$ 

Globals:

Cov\_man20 Cov\_man30

x\_sh\_LO x\_sh\_HI y\_sh\_LO y\_sh\_HI

## Description:

Tests if predicted position falls within a shadow region. Sets flag to 1 if in shadow. [The shadow zones were specified as a set of rectangular tiles by the scenario generator. The array x\_sh\_LO, x\_sh\_HI, y\_sh\_LO, and, y\_sh\_HI specify low and high positions of each time.]

Test\_In\_Shadow

Calling Module:

Shadow\_Test

Called Modules:

None

Inputs:

Z\_p Prediction state vector (x;vx;ax;y;vy;ay)
x\_sh\_LO Array specifying low x position of shadow tiles
x\_sh\_HI Array specifying high x position of shadow tiles
y\_sh\_LO Array specifying low y position of shadow tiles
y\_sh\_HI Array specifying high y position of shadow tiles

Outputs:

In\_Shadow

In shadow status flag  $(1 \Rightarrow \text{in shadow})$ 

Globals:

None

Description:

Tests if predicted position falls within any of the shadow tiles that were specified by the scenario generator.

Discrete\_Test

Calling Module:

Run\_Tracker\_8

Called Modules:

E\_Discrete\_Test

Inputs:

 $Z_p$ 

Prediction state vector

gate\_case

Gate case flag (1:3)

ang\_pred

Angle (rad) of predicted point

semi\_rng\_T semi\_crng\_T Semi axis length of along range ellipse Semi axis length of cross range ellipse

ang\_trk

Angle (rad) of track

semi\_trk\_T semi\_ctrk\_T

Semi axis length of along track ellipse

Semi axis length of cross track ellipse

Outputs:

In\_Discrete

Discrete capture flag (1 => discrete present)

Globals:

None

Description:

Tests if discrete point falls within either of two gates oriented along/across range or along/cross track.

# Equations:

```
(gate\_case = 1)
```

Each discrete point is tested for inclusion in a single ellipse, centered on the predicted point, and oriented along range/cross range. The semi axes are given by semi\_rng\_T and semi\_cross\_T.

```
(gate\_case > 1)
```

Each discrete point is tested for inclusion if either of two ellipses, both centered on the predicted point. The first ellipse is the same as defined above. The second ellipse is oriented along track/cross track and has semi axes given by semi\_trk\_T and semi\_ctrk\_T.

**E\_Discrete\_Test** 

Calling Module:

Discrete\_test

Called Modules:

Test\_E\_Gate

Inputs:

 $Z_p$ 

Prediction state vector (x;vx;ax;y;vy;ay)

ang\_rotn

Rotation angle (rad) of ellipse gate wrt radar cs

semi\_along semi\_across Semi axis length of gate along rotated x Semi axis length of gate along rotated y

Outputs:

In\_Discrete

Discrete inclusion flag (1 => discrete in)

Globals:

Ndiscrete X\_D\_Vec Y\_D\_Vec

Description:

Tests if any of a set of discrete points falls within an elliptical gate: (1) centered on the predicted point, (2) oriented at an angle "ang\_rotn" wrt radar coordination system, (3) having semi axes lengths of semi\_along along the rotated x axis and of length semi\_across along the rotated y axis.

The discrete locations were specified by the scenario generator and given here by the arrays X\_D\_Vec and Y\_D\_Vec.

TR\_Assoc\_Max\_T

Calling Module:

Run\_Tracker\_8

Called Modules:

cmp\_track\_age

Inputs:

Corr

Binary correlation matrix (trks, reps)

Dist

Distance matrix (trks, reps)

NAT\_in Nrep\_in

Number of active tracks in Table\_T Number of reports from current scan

scan

Current scan

Outputs:

Update

Binary array of updated tracks (1 => updated)

unAssoc unused

Binary array of unassociated tracks Binary array of unused reports

Asgn\_Reps

Array of reports assigned to each track

Globals:

Table\_T

## Description:

Assigns unique reports to corresponding track. If a report is common to multiple tracks then it is assigned to the oldest track.

TR\_Assoc\_Min\_D

Calling Module:

Run\_Tracker\_8

Called Modules:

cmp\_track\_age

Inputs:

Corr

Binary correlation matrix (trks, reps)

Dist

Distance matrix (trks, reps)
Number of active tracks in Table\_T

NAT\_in Nrep\_in

Number of reports from current scan

scan

Current scan

Outputs:

Update

Binary array of updated tracks (1 => updated)

unAssoc

Binary array of unassociated tracks

unused

Binary array of unused reports

Asgn\_Reps

Array of reports assigned to each track

Globals:

Table\_T

Description:

Assigns unique reports to corresponding track. If multiple reports are common to a given track then the closest is assigned to the track.

cmp\_track\_age

Calling Module:

TR\_Assoc\_Max\_T

Called Modules:

None

Inputs:

trk

Track index into Table\_T

scan

Current scan

Outputs:

age

Track age since first became firm

Globals:

Table\_T

Description:

Computes age of a track in scan units. Age is defined as time since track became firm.

get\_track\_ang

Calling Module:

Run\_Tracker\_8

Called Modules:

None

Inputs:

 $Z_p$ 

Prediction state vector

Z\_s\_last

Smoothed state vector (last update)

Outputs:

ang\_trk

Angle of track (radians)

Globals:

None

Description:

Computes track angle in radians with respect to the radar coordinate system.

get\_pred\_ang

Calling Module:

Run\_Tracker\_8

Called Modules:

None

Inputs:

Z\_p

Prediction state vector

Outputs:

ang\_pred

Prediction of Angle

Globals:

None

Description:

Computes angle of predicted point with respect to the radar coordinate system.

update\_error

Calling Module:

Run\_Tracker\_8

Called Modules:

None

Inputs:

N\_Hits

Number of times track captured a report

Z\_tru

True state vector

Z\_p

Prediction state vector

TID

Track ID number

Outputs:

mean\_error

Position error (predicted - true) averaged over N\_Hits

sigma\_error

Standard deviation of position error

Globals:

SUM1\_ERROR

SUM2\_ERROR

## Description:

Computes running mean and standard deviation of position error between predicted and true values as a function of track ID number. Stores running first and second moments in global buffers SUM1\_ERROR and SUM2\_ERROR.

Load\_P\_DET

Calling Module:

Run\_Tracker\_8

Called Modules:

None

Inputs:

Ntk\_max

Number of tracks in P\_DET buffer

scan

Current scan index

N\_HITS

Number of captures for track

**N\_EVENTS** 

Number of captures plus misses for track

Outputs:

None

Globals:

Table\_T\_P\_DET

Description:

Computes fraction of captures for specific track over its evolution. Stores results in global buffer P\_DET.

Load\_dBuf\_4

Calling Module:

Run\_Tracker\_8

Called Modules:

get\_Table\_Trk\_4

Inputs:

Ntrk

Current number of tracks

dBuf\_last\_cnt

Number of dropped HP tracks in buffer dBuf at last scan

Outputs:

 $dBuf\_cnt$ 

Number of dropped HP tracks in buffer dBuf currently

Globals:

dBuf

Table\_T

DROPPED TENT FIRM

DP LP

## Description:

Updates the high priority dropped track buffer each scan. The buffer dBuf has three components: (time, x position, y position)

plot\_dBuf

Calling Module:

Run\_Tracker\_8

Called Modules:

None

Inputs:

dBuf\_new

plot\_vec

Counter in dropped track buffer Min and max s and y values of plot space

Outputs:

None

Globals:

dBuf

Description:

Plots dropped high priority tracks each scan.